

—演講題目—

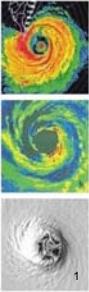
颱風、氣候與災害



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你快樂嗎？一個簡單的生涯規劃動力系統

u : 快樂指數
 x : 考試作業量
 y : 玩魔獸的時間

天縱英明的資優生	<0	>0	<0	>0
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$\frac{\partial u}{\partial x} > 0$ 考試越多越快樂
 $\frac{\partial u}{\partial y} < 0$ 電動越玩越不快樂

$\frac{\partial u}{\partial x} < 0$ 考試越少越不快樂
 $\frac{\partial u}{\partial y} > 0$ 玩魔獸的時間越多越不快樂

人的個性

個性+境遇=人生
相形不如論心
論心不如則術
形不勝心
心不勝術

荀子非相

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讀 算 寫

幾何
代數
微積分
電腦計算繪圖
數學建模/科學計算
Mathematical Modeling
Scientific Computing

+	-	\times	/
加、減		乘、除	
線性		非線性	
		大題大作	小題大作

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Fovell, 2008 高雄

This model will be a simplification and an idealization, and consequently a falsification. It is to be hoped that the features retained for discussion are those of greatest importance in the present stage of knowledge.

Turing The Chemical Basis of Morphogenesis

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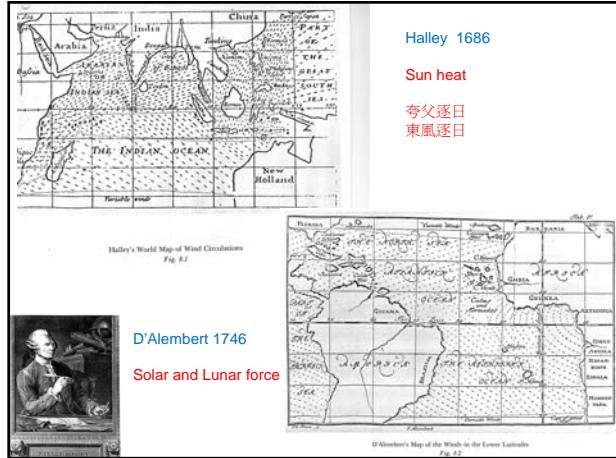
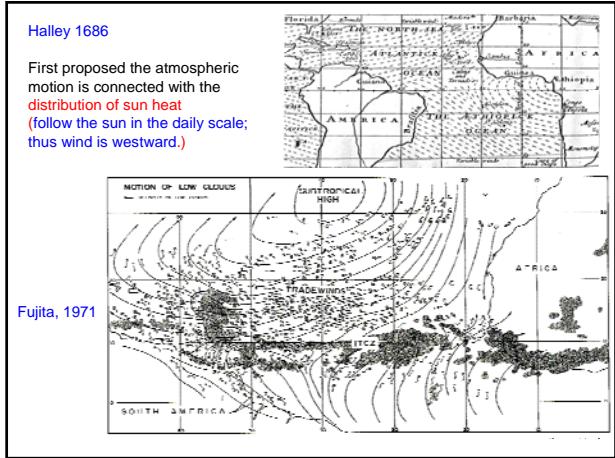
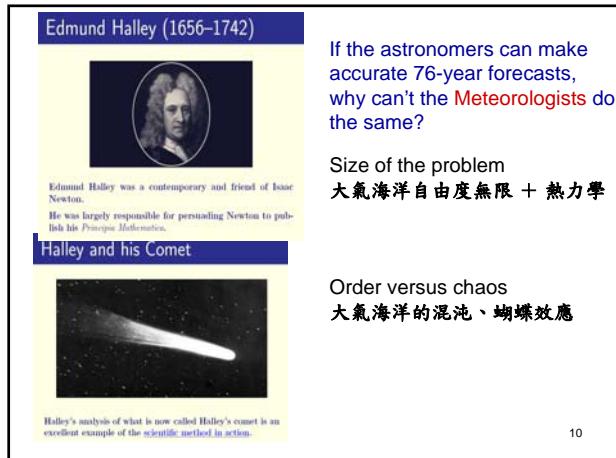
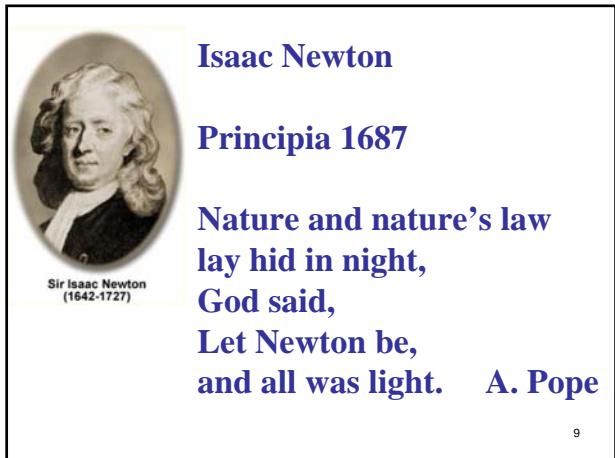
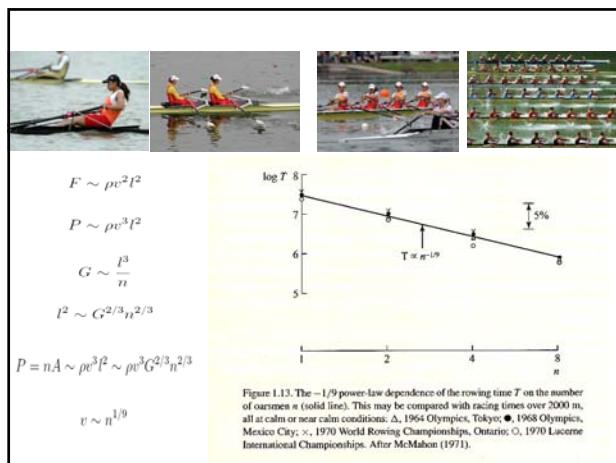
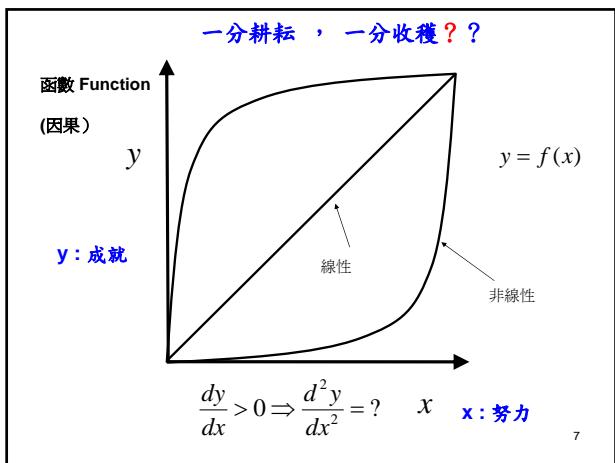
“Six monkeys, set to strum unintelligently on typewriters for millions of years, would be bound in time to write all the books in the British Museum.” Huxley

君子致用在乎經邦，經邦在乎立事，立事在乎師古，師古在乎隨時。必參古今之宜，窮終始之要，始可以度其古，中可以行於今。道典

共49個字，假設中文常用字為1000字，共有 10^{147} 個選擇

地球歷史 10^{18} sec
 10^{10} 一百億隻猴子在打字，假設每秒鐘打一萬字 10^4 ，
 $10^{10} \times 10^{18} \times 10^4 = 10^{32}$
 $10^{32} / 10^{147} = 10^{(-115)} \sim 0$ 機率為零，不可能的巧合！

研究學問是苦心孤詣的事業！ 不要人云亦云！



Euler's Equations for Fluid Flow



Leonhard Euler, born on 15 April, 1707 in Basel. Died on 18 September, 1783 in St Petersburg.
Euler formulated the equations for incompressible, inviscid fluid flow:

$$\frac{\partial \mathbf{V}}{\partial t} + \mathbf{V} \cdot \nabla \mathbf{V} + \frac{1}{\rho} \nabla p = \mathbf{g},$$

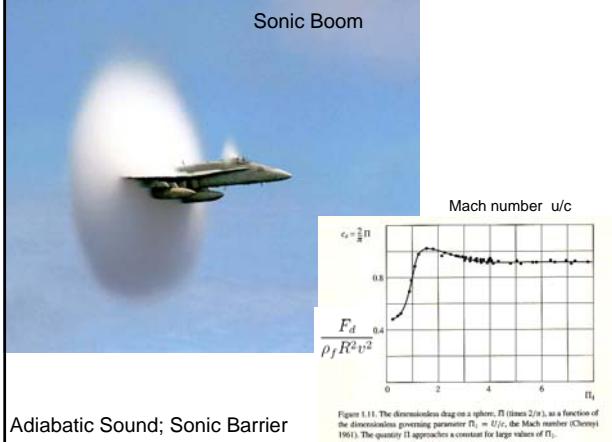
$$\nabla \cdot \mathbf{V} = 0$$

流體力學之父

Partial Differential Equations
偏微分方程式 PDE

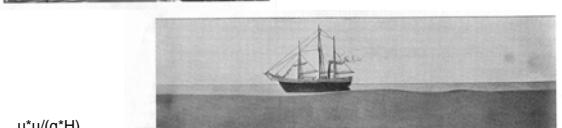
非線性

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Dead-water near the coast

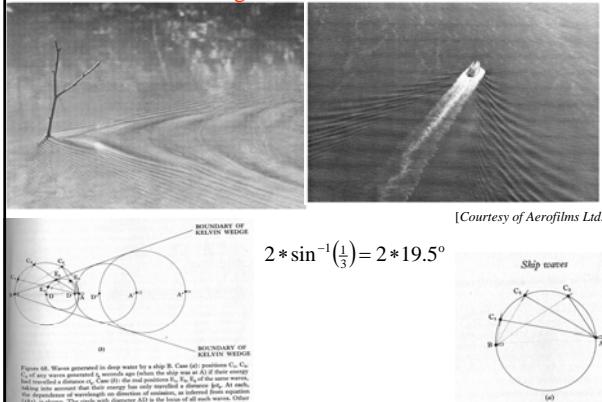
Wave drag problem



$u^* u / (g^* H)$

Fig. 4.2. (a) Surface "vicks" showing the presence of internal waves in the wake of a ship in Bute Inlet, British Columbia. The vessel was traveling at 0.5 m s^{-1} in a surface layer of almost fresh water only slightly deeper than its 3.4 m draft. The internal waves caused horizontal motion at the surface that affects the ripple pattern and so renders the internal wave pattern visible at the surface during calm conditions. (Photo courtesy of Defence Research Establishment Pacific, Victoria, British Columbia.) (b) A laboratory experiment (from Ekman (1904)) showing internal waves being generated by a model ship. The tank is filled with two fluids of different density, the heavier one being dyed to make the interface clearly visible. The model ship (the superstructure of the "Fram" has been drawn in subsequently) is towed from right to left, causing a wave of waves on the interface.

Kelvin wedge deep water waves



D'Alembert 1746

Math. Model for Atmospheric Motion in aqua-planet
(Won the 1746 Berlin Academy's Award; Euler's endorsement)

Solar and Lunar Force

Fourier 1768-1830

Why the earth not heating up when receive sun energy continuously?

Hadley (1685-1758)

Distribution of sun heating (north and south; seasonal scale)

Earth rotation (conservation of angular momentum)

Thomson (1857)

Ferrel (1859)

Centrifugal force

Coriolis 1835

Heat emission or diffusion (by IR)

His calculations showed a very cold surface (No green house effect)

Arrhenius 1896

CO_2 green house effect, but were dismissed by scientists [WHY??]

Ideal Gas Law Equation of State 理想氣體方程

- 1662, Boyle law, $PV = c$ when $T = c$.
- 1787, Charles law, $V/T = c$ when $P = c$.
- 1803, Gay-Lussac law, $P/T = c$ when $V = c$.
- 1811, Avagadro, 1 mole gas is 22.4 l in volume.

Universal Gas Constant
 $R^* = 8314.3 \text{ J}/(\text{deg. kmol})$

$$PV = n R^* T$$

$$PV = m/M R^* T \quad P = m/V R^*/M T$$

$$P = \rho R T, \quad R = R^*/M$$

$$R_d = 287 \text{ J}/\text{deg. kg} \quad (R^*/M_d)$$

$$R_v = 461 \text{ J}/\text{deg. kg} \quad (R^*/M_v)$$

$$P = f(V, T)$$

$$V = h(P, T)$$

溫度可以改變壓力或體積，
熱可以做功

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Estimate Avogadro's Number

Benjamin Franklin (1773)

(1) Molecular size

$$l = \frac{V}{A} = \frac{4.9 \text{ cm}^3}{2.0 \times 10^7 \text{ cm}^2} = 2.4 \times 10^{-7} \text{ cm}$$

(2) Number of molecules

$$N = \frac{A}{l^2} = \frac{2.0 \times 10^7 \text{ cm}^2}{(2.4 \times 10^{-7} \text{ cm})^2} = 3.5 \times 10^{20} \text{ molecules}$$

(3) Mass of the oil

$$m = V \times D = 4.9 \text{ cm}^3 \times 0.95 \frac{\text{g}}{\text{cm}^3} = 4.7 \text{ g}$$

(4) Number of moles of oil

$$\text{Moles of oil} = \frac{4.7 \text{ g}}{200 \text{ g/mol}} = 0.024 \text{ mol}$$

(5) Avogadro's number

$$\text{Avogadro's number} = \frac{3.5 \times 10^{20} \text{ molecules}}{0.024 \text{ mol}} = 1.5 \times 10^{23}$$

Now we know: $N_A = 6.022142 \times 10^{23} / \text{mol}$

Development of Thermodynamics 热力学
19 century

第一定律 能量作用，能量守恒
First law: Energy is what makes it go and energy is conserved.

$\Delta Q = \Delta U + \text{WORK}$ 能量=内能+功
Second law: Entropy tells it where to go!
第二定律 時間之矢，自然單向

Joule, Rudolf Clausius, Lord Kelvin and others

宏观 微观
Macro --- Micro

Classical and Statistical Thermodynamics 統計熱力学

Ludwig Boltzmann, 1844-1906, whose work led to an understanding of the macroscopic world on the basis of molecular dynamics.

$S = k \log W$

雲微物理
Precipitation

Enthalpy
Entropy
Gibbs Free energy

Planck, Unwilling Revolutionary: the idea of quantization

1900

Hall of Fame in Science

Gravitational Law

Blackbody Radiation

$E=MC^2$

Figure 8.7 Spectra of emitted intensity $B_\lambda(T)$ for blackbodies at several temperatures, with wavelength of maximum emission $\lambda_m(T)$ indicated.

黑體輻射公式

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19 century weather map

16 January 1888
7 am Eastern Time
Vilhelm Bjerkenes (1862-1951)

Maxwell 電磁波

Modern weather map

The Ultimate Problem in Meteorology Bjerkenes 1911 氣象的終極問題

I The Present state of the atmosphere must be characterized as accurately as possible. 正確的觀測大氣現狀 [多重時空尺度]

II The intrinsic laws, according to which the subsequent states develop out of the preceding ones, must be known. 正確的大氣運作規律

Numerical Weather Prediction 數值天氣預報
[第一部電腦ENIAC, EBV model, 1950]
The Observation component 觀測
The diagnostic or analysis component 診斷分析
The prognostic component 預報

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科氏力(18 19)

$$\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} + w \frac{\partial u}{\partial z} - fv = -\frac{1}{\rho} \frac{\partial p}{\partial x} + \nu \nabla^2 u$$

Momentum Conservation (18) $\frac{\partial v}{\partial t} + u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} + w \frac{\partial v}{\partial z} + fu = -\frac{1}{\rho} \frac{\partial p}{\partial y} + \nu \nabla^2 v$

$$\frac{\partial w}{\partial t} + u \frac{\partial w}{\partial x} + v \frac{\partial w}{\partial y} + w \frac{\partial w}{\partial z} = -\frac{1}{\rho} \frac{\partial p}{\partial z} - g + \nu \nabla^2 w$$

Mass conservation (18) $\frac{\partial \rho}{\partial t} + \frac{\partial up}{\partial x} + \frac{\partial vp}{\partial y} + \frac{\partial wp}{\partial z} = 0$

Energy conservation (19) $\frac{\partial \theta}{\partial t} + u \frac{\partial \theta}{\partial x} + v \frac{\partial \theta}{\partial y} + w \frac{\partial \theta}{\partial z} = Q$

Equation of State(17,18,19) $p = \rho R_A T, \quad \theta = T \left(\frac{p_0}{p} \right)^{\frac{R_A}{C_p}}$

Radiation 大氣輻射 (19,20)
Moisture Latent heat
雲物理 (19,20)

問蒼茫大氣，誰主浮沈？ (19)
質量、動量、能量與大氣狀態方程式

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Lewis Fry Richardson, 1881–1953.



During WWI, Richardson computed by hand the pressure change at a single point.

It took him two years !

His ‘forecast’ was a catastrophic failure:

$\Delta p = 145 \text{ hPa}$ in 6 hours

His method was unimpeachable.

So, what went wrong?

Peter Lynch



$$\frac{df}{dx} \rightarrow \frac{f(x + \Delta x) - f(x - \Delta x)}{2\Delta x}$$

$$\frac{dQ}{dt} \rightarrow \frac{Q^{n+1} - Q^{n-1}}{2\Delta t} = F^n$$

13x13=169 個ODE

169 自由度

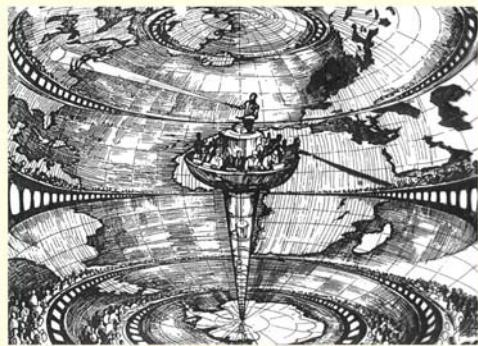
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first weather forecast - ENIAC, 1950



In front of the Eniac, Aberdeen Proving Ground, April 4, 1950, on the occasion of the first numerical weather computations carried out with the aid of a high-speed computer. 27

Richardson's Dream



Richardson's Forecast Factory (A. Lannerback).
Dagens Nyheter, Stockholm. Reproduced from L. Bengtsson, ECMWF, 1984

64,000 Computers: The first Massively Parallel Processor

The ENIAC
Electronic Numerical Integrator and Computer



18000 vacuum tubes
70000 resistors
10000 capacitor
6000 switches

140 K Watts power

No high-level language
Assembly language

500 Flops
Function Table 0.001 s

3,700,000,000 times slower than current day large computer

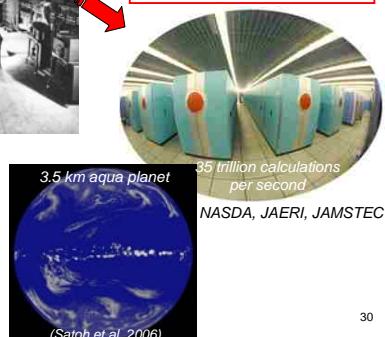
第一部電腦 氣象預報

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ENIAC – late 40s

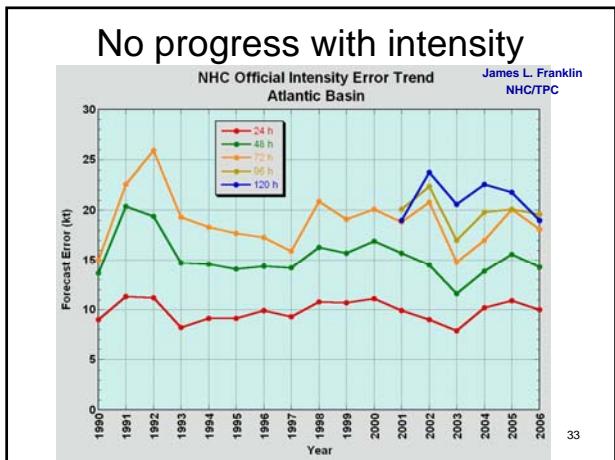
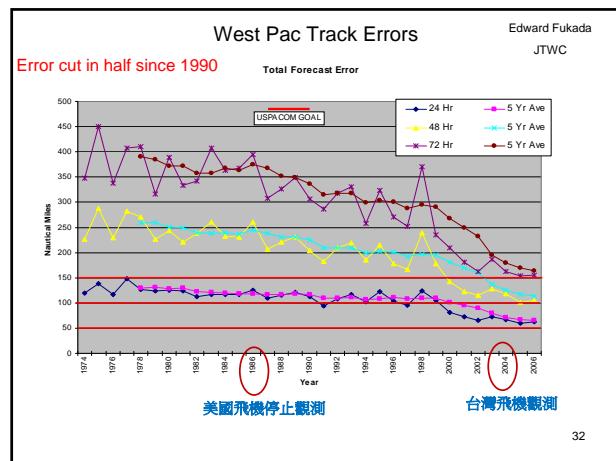
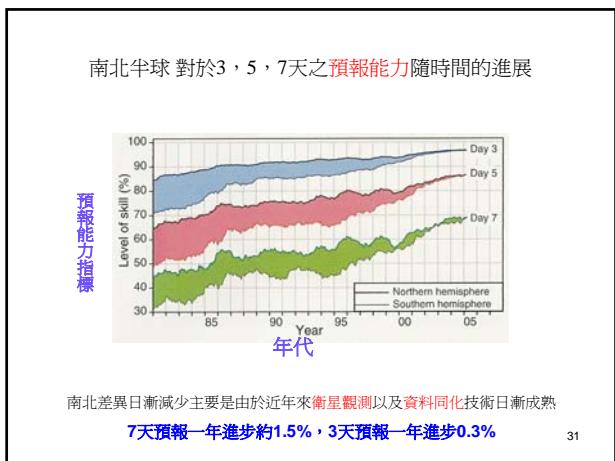


Earth Simulator -- 2002



3.5 km aqua planet
85 trillion calculations per second
NASDA, JAERI, JAMSTEC

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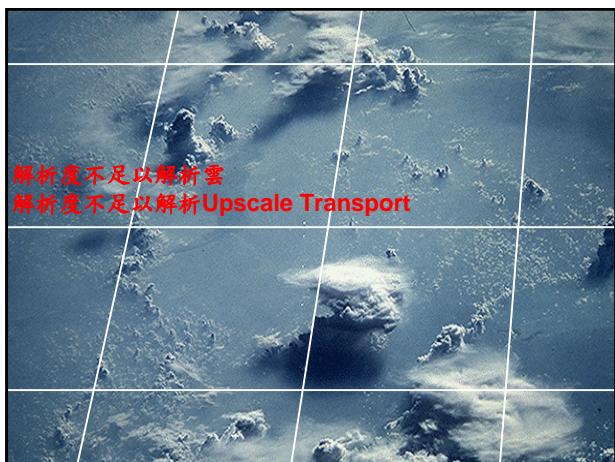
颱風潛熱與其它能量的比較

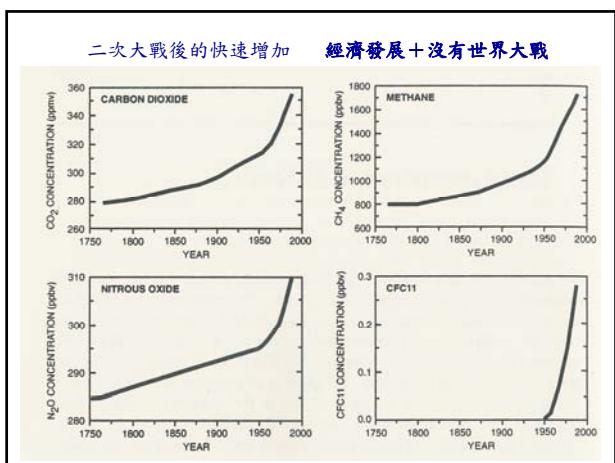
賈伯颱風的全台灣平均總雨量為400mm
 $400 \text{ mm} = 0.4 \text{ m}$
 $0.4 \text{ m} * 1000 \text{ kg m}^{-3} * 2.5 \times 10^6 \text{ J kg}^{-1} = 10^9 \text{ J m}^2$
 $10^9 \text{ J m}^2 * 3.5 \times 10^{10} \text{ m}^2 = 3.5 \times 10^{19} \text{ J} \sim 10^{20} \text{ J}$

${}_0^1\text{n} + {}^{235}_{92}\text{U} \rightarrow {}^{142}_{56}\text{Ba} + {}^{91}_{36}\text{Kr} + {}^{3}_{0}\text{n}$
 $1.68 * 10^{13} \text{ J/mol} \Rightarrow 1.46 \times 10^{25} \text{ kg U}^{235} (6 * 10^6 \text{ mol})$

能量估計值	備註
賈伯颱風降雨總潛熱能量 10^{20} J	可使台灣整層大氣增溫100度
台灣一年用電量 $5 \times 10^{17} \text{ J}$	需數百年用電量才相當
全世界核子彈爆炸釋放能量 $2 \times 10^{19} \sim 2 \times 10^{20} \text{ J}$	與賈伯颱風同等級
核戰後燃燒釋放能量 $2 \times 10^{20} \text{ J}$	與賈伯颱風同等級
地球一天接受的太陽能量 $1.5 \times 10^{22} \text{ J}$	數百個賈伯颱風
Tunguska隕石撞地 球（西元1908年， 西伯利亞） 10^{16} J	賈伯颱風的萬分之一
火流星撞地球（恐龍滅絕？） $4 \times 10^{23} \text{ J}$	數千個賈伯颱風

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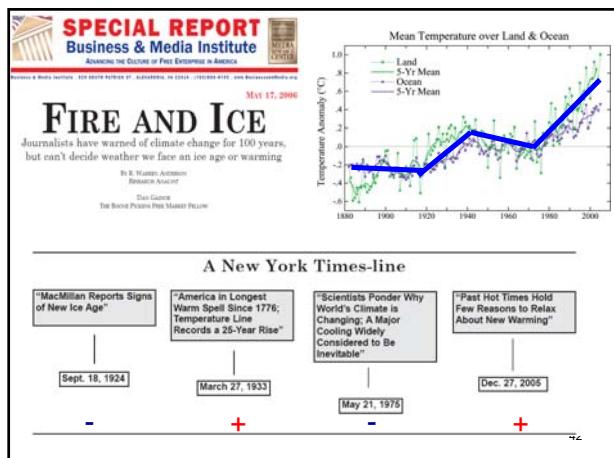
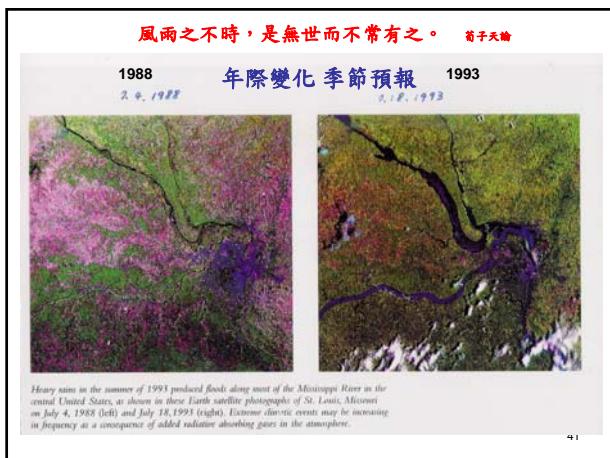
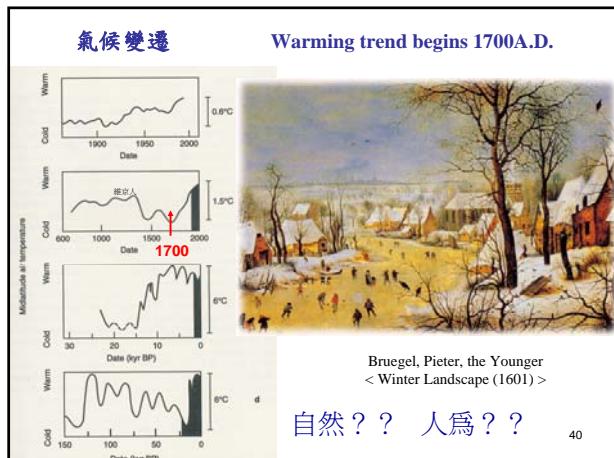
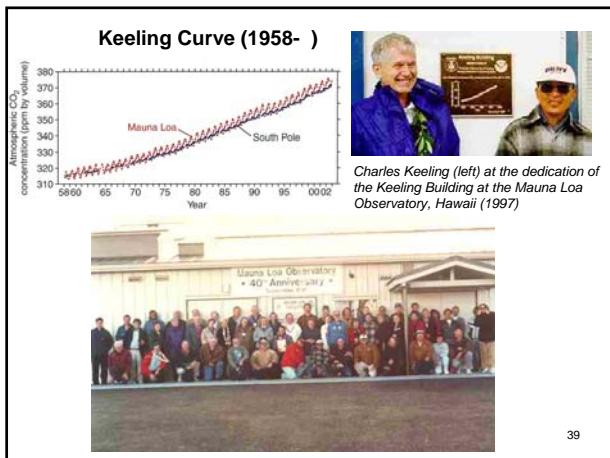


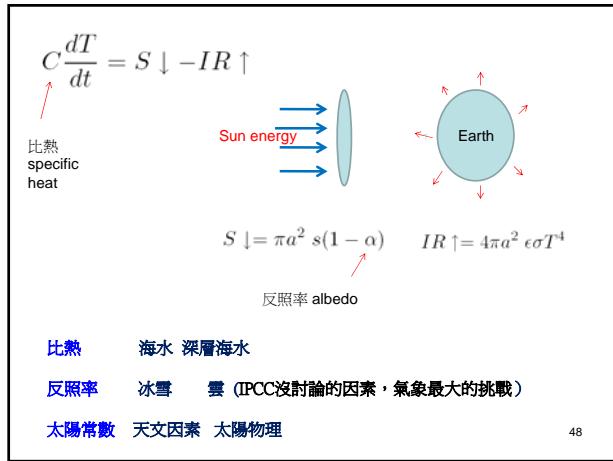
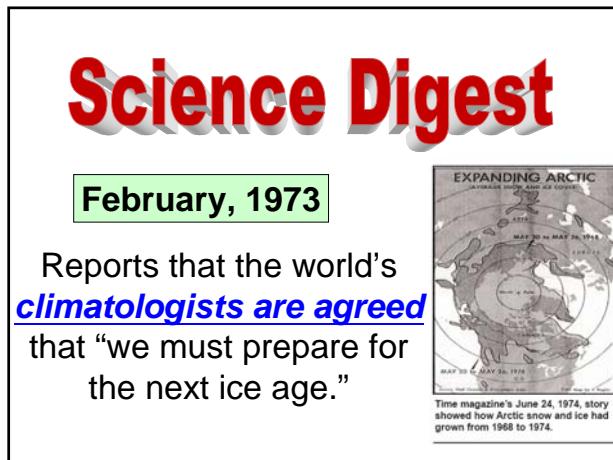
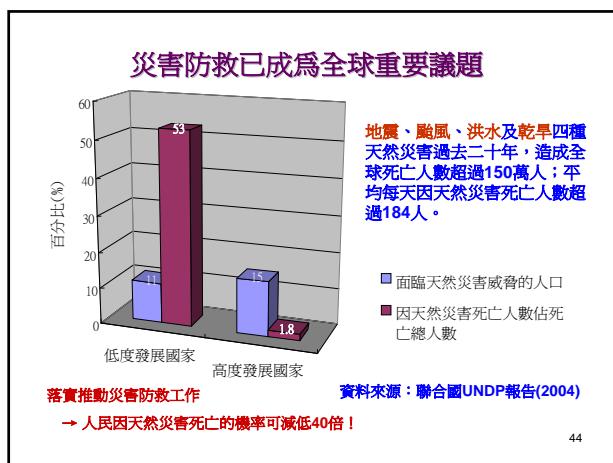
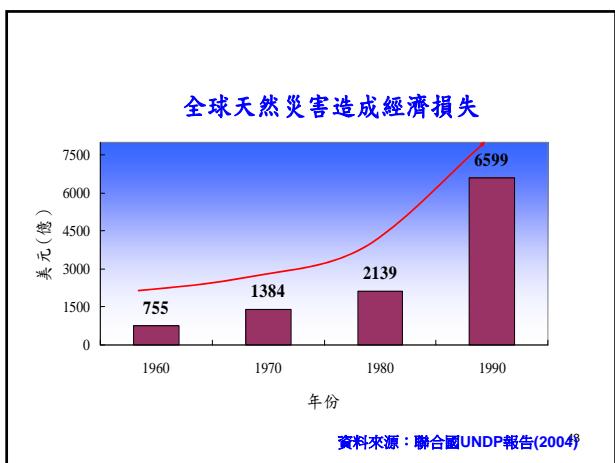


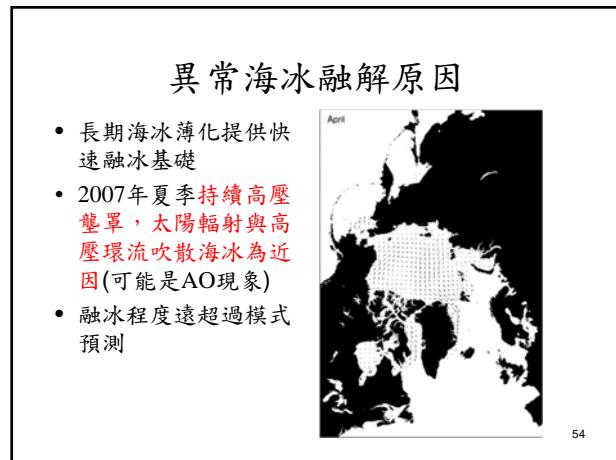
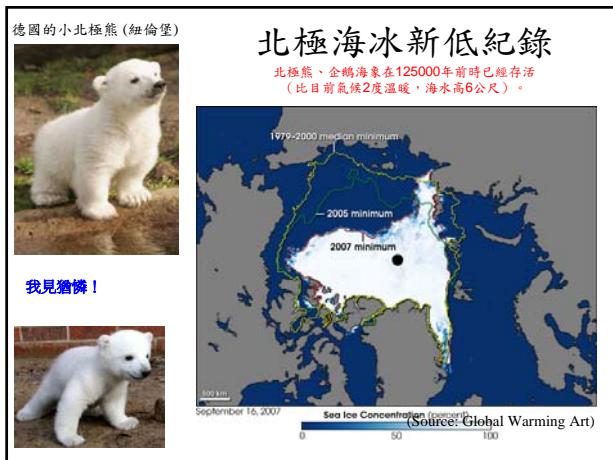
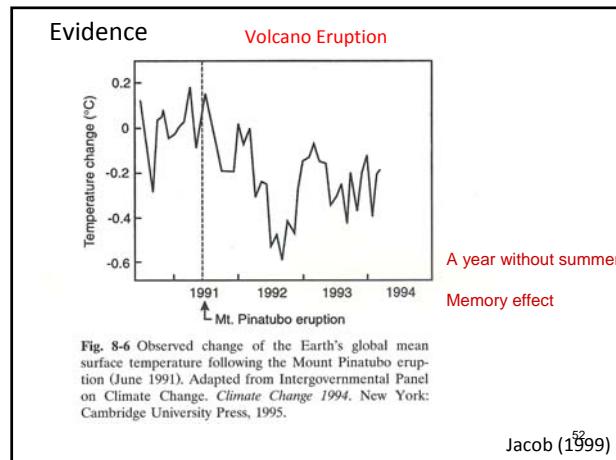
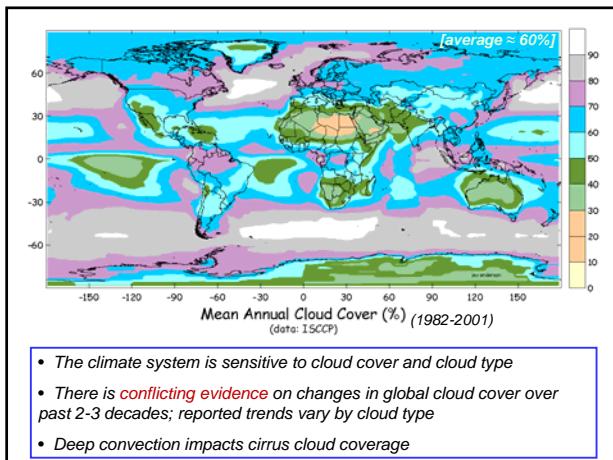
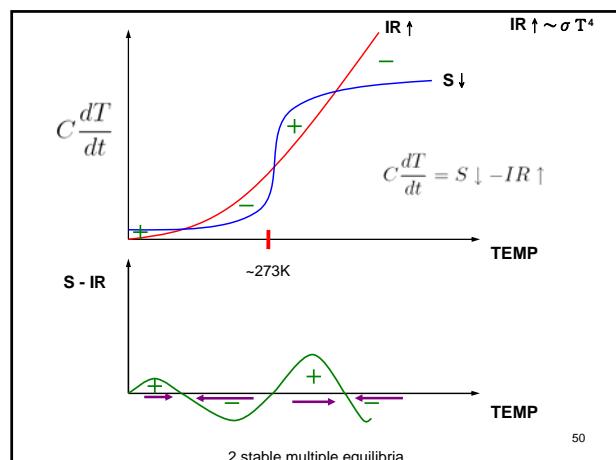
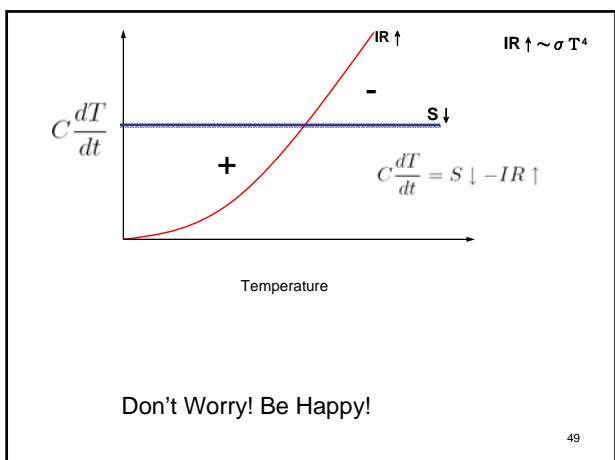
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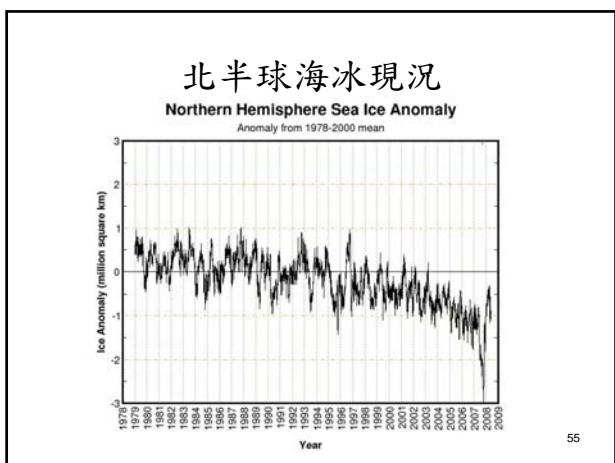


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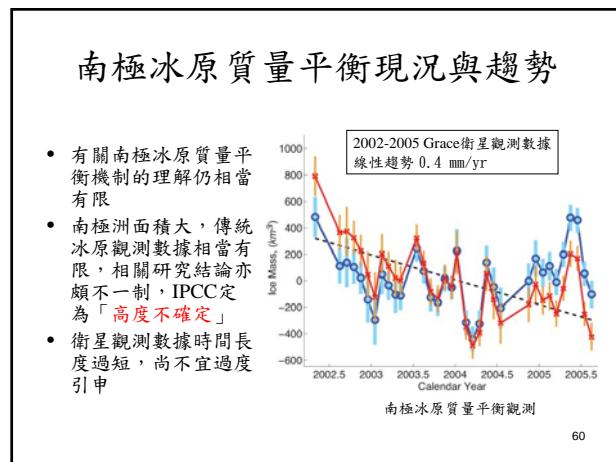
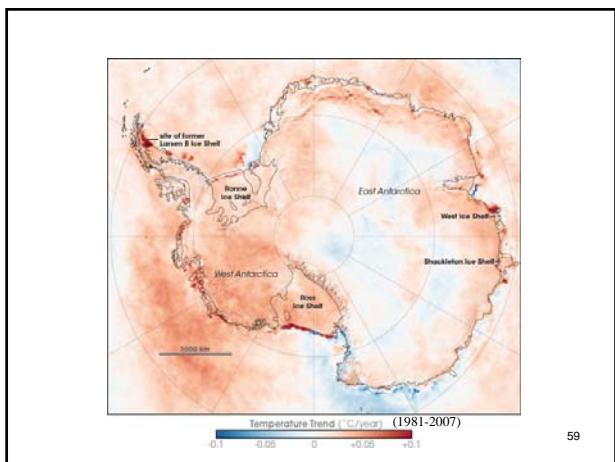
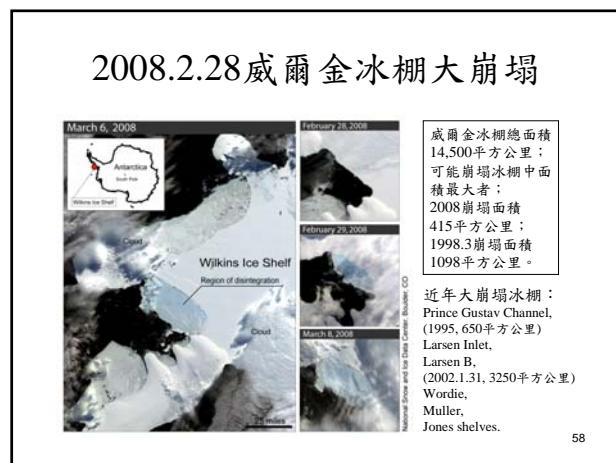
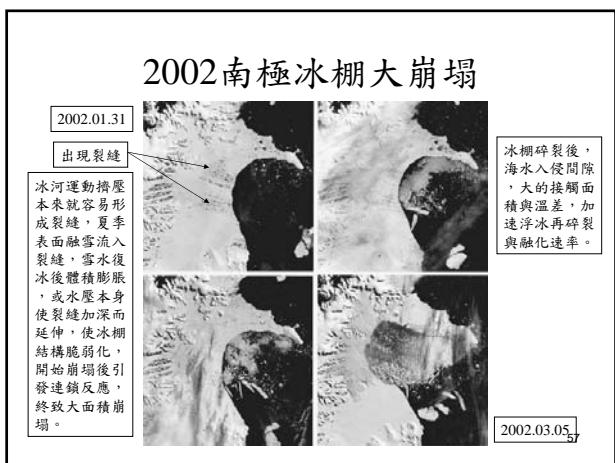


2007北極海冰極小值的啟示

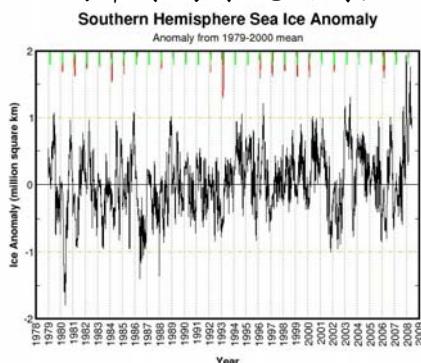
「2008九月前北極冰恐消失」2008.6.28中時
“chances are 50% and 50%”

- 2007極小值遠低於所有模式預測
 - 再次顯示我們對氣候(天氣)系統理解的不足
 - 也可能再回復
 - 未來持續縮小趨勢機會很高
- 北極海冰覆蓋面積大，對全球氣候應有影響
 - 短期變化應該與全球暖化無直接關連
 - 所謂氣候自然變異幅度絕不可輕忽
 - 長期趨勢仍是值得關注的全球暖化指標
- 北極海冰變化尚無影響全球深海循環的證據

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南半球海冰現況對照



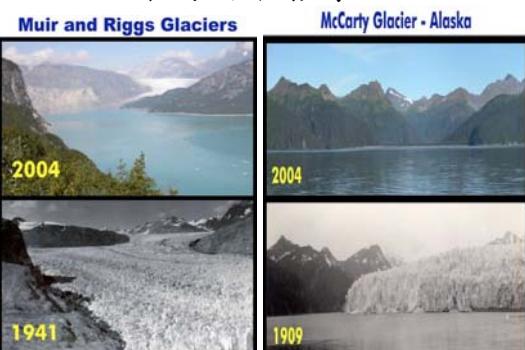
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高山冰河退縮問題

- 高山冰河退縮常被作為全球暖化指標
 - 「不願面對的真相」令人震撼的「暖化指標」之一
- 冰河是研究古氣候的重要資訊來源
 - 冰河中永凍的古生物與鑽探分析的冰核保留豐富資訊
- 高山冰河同時是自然生態與人類活動的重要淡水來源
 - 冰河是天然水庫—主要江、河常源自高山冰河
 - 「瑞雪兆豐年」—冰河釋出的水可能是部分地區唯一或主要水源

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冰河退縮影像



冰河退縮影像



全球海平面上升議題

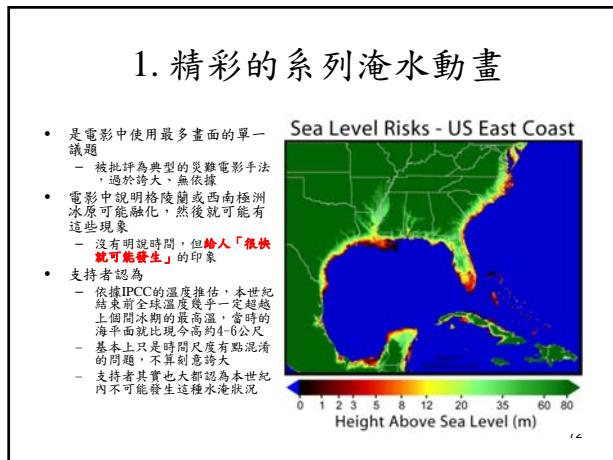
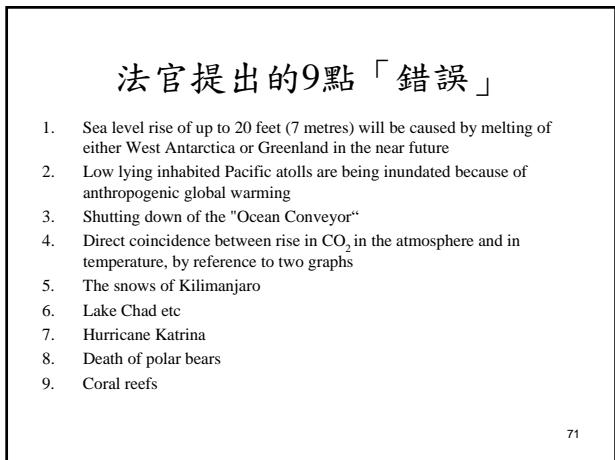
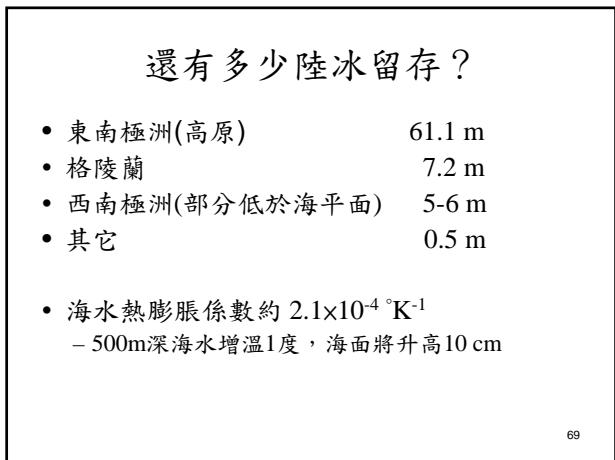
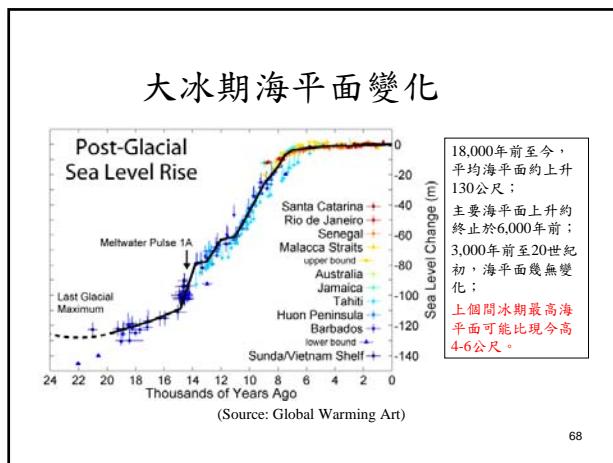
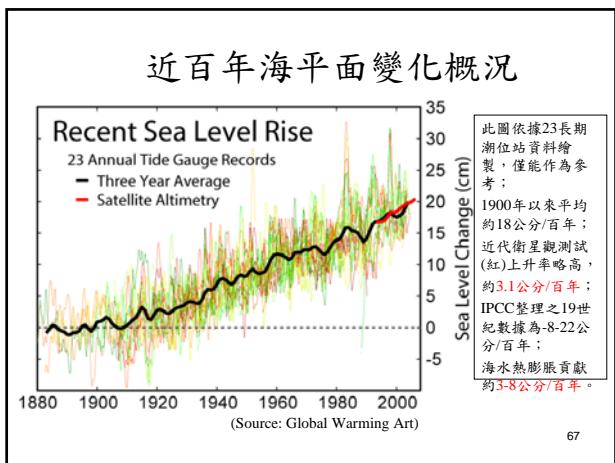
- 符合直覺式的全球暖化聯想
 - 一般民眾最能體會、最關心的議題
 - 「**大洪水**」的聯想（**諾雅方舟？**）
- 全球暖化論述最嚴重的潛在威脅
 - 人類主要的居住、生產、經濟活動都在沿海的低海跋區域
 - 幾乎不分國家或地區的開發程度都可能受嚴重衝擊
 - 沿岸區域是地球生態系統最豐富的區域之一
 - 近岸地形對海平面變化敏感，過於快速的海岸線變化恐造成生態浩劫
- 陸地海跋高度係以平均海平面為基準

65

平均海平面估算的困難

- 海平面變化含有**各種時間尺度**
 - 幾乎是連續的頻譜，量測與頻譜分離都不容易
- 量測點不足、時間長度有限
- **早期量測係以陸地為基準的相對值**
 - 地殼變動因素複雜、各地情況也不一致
- 海平面升降具有明顯區域特性
 - 受區域氣候、洋流、海水溫度影響

66



太平洋島國必須逃難

- 高爾以上哇魯為例，說明這個島國民因此須要逃難到紐西蘭
 - 被批評說「根本沒這回事」
- 電影中是接在2002年極冰棚大崩塌之後，說明陸冰也可能崩塌而造成非預期的海平面上升，像土哇魯這樣的地方就因此需要逃難到紐西蘭
- 事實是土哇魯的確因為「地層下陷」與風暴造成的海岸侵蝕而使生存環境越來越惡劣
 - 和全球暖化沒有直接相關
 - 電影之後，土哇魯剛好巧合的和紐西蘭討論租地的事
 - 支持者認為只是「示意」，用個方便的例子，可能是錯誤選擇，但無傷大雅



聖嬰年西太平洋海水高度會降~50 cm

73

3. 深海循環中斷



- 被批評花太多時間說明一個很不可發生的情況，會發生的話也要數百年至數千年之後
- 電影中直接點出了「新仙女木事件」，目的是在解釋一個可能引發氣候劇烈變化的物理機制，有點像是在解釋電影「明天過後」的邏輯，但比較科學多了
- 事實上NOAA和IPCC都有正式聲明，這個氣候變異機制「很可能」在未來百年內發生
 - 支持者認為這是個很重要的氣候變異機制，值得介紹
 - 這個機制還有許多未知的細節，學理上其實無法完全排除在未來發生的可能，只是時間尺度的確應在百年以上
- 這是我最喜歡的氣候變異理論之一，支持！

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Uncertainty over weakening circulation

Petr Chylek
Scripps Institution of
Oceanography
La Jolla, San Diego, California

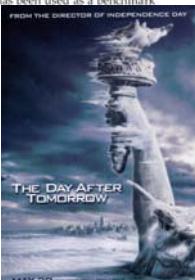
Bryden and Longworth *Nature* 2005

1957 $22.9 \pm 6 \text{ SV}$

2004 $14.8 \pm 6 \text{ SV}$

Net $8.1 \pm 6 \text{ SV}$

$$1 \text{ SV} = 10^6 \text{ m}^3 \text{s}^{-1}$$

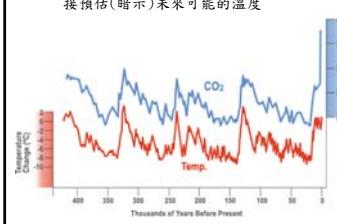


correct result. It is a mystery how such an error was missed by Levi and by the editors and reviewers of the original paper. The observed change of 8.1 Sv is well within the uncertainty of the measurement. The correct conclusion from

$$8.1 \pm 12 \text{ SV}$$

4. 溫度隨CO₂濃度「高升」

- 被批評誤導CO₂濃度和溫度變化的因果關係
 - 這是真正理論氣候學者討論最多的主題
- 電影中先說明兩者65萬年來的明顯相關性，然後以預期的CO₂濃度直接預估(暗示)未來可能的溫度



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5. 吉利馬札羅冰河 Local change or Global change??

- 媒體特別鍾情吉利馬札羅山，法官認為不應妄下結論，該冰河消失原因與全球暖化的關係未明
- 電影中這是一系列冰河退縮對比中的一景
- 吉利馬札羅山冰河退縮的真正原因的確尚無定論
 - 冰河退縮是個全球性普遍的趨勢，但是也有冰河持續發展中，而每條冰河變化的因素也都不盡相同，此例用來說明冰河退縮現象還可以，用來說明全球暖化的結果就太勉強了
 - 現今殘存的吉利馬札羅山冰河至少已存在12,000年以上，這個變化的原因應該個值得關心的問題

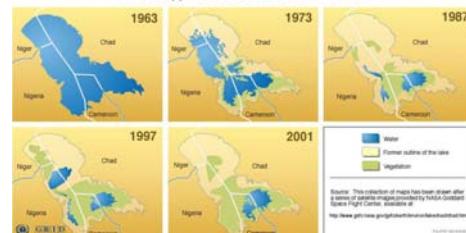


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一個「拜錯菩薩燒錯香」的例子？

6. 乾涸中的查德湖

The Disappearance of Lake Chad in Africa



- 被批評不應當成「暖化後果」的例證，實情應該是人口增加、過度取用灌溉水源及區域氣候變遷影響
- 電影中是用來說明暖化的結果，「有些地方會發生洪水、有些地方會產生乾旱」
- 是水資源使用的問題，不過部分全球暖化模擬的確預測該區降水減少

78

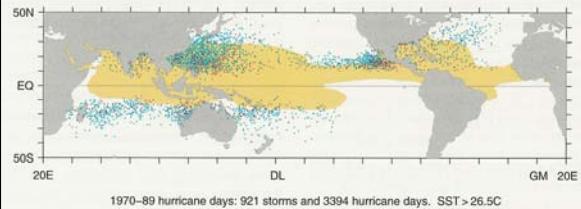
7. 卡翠那颶風

- 被批評不應把卡翠那颶風在紐澳良造成的災難歸因於全球暖化，這已是科學界的共識
- 電影中高爾未明說，但邏輯延續上的確會被解讀為「這就是暖化的後果之一」
- 任何獨立天氣事件都不應直接被歸因於全球暖化，IPCC也接受這個觀點**

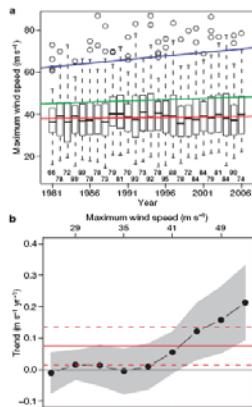


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颶風、颶風與全球暖化的關係？



80

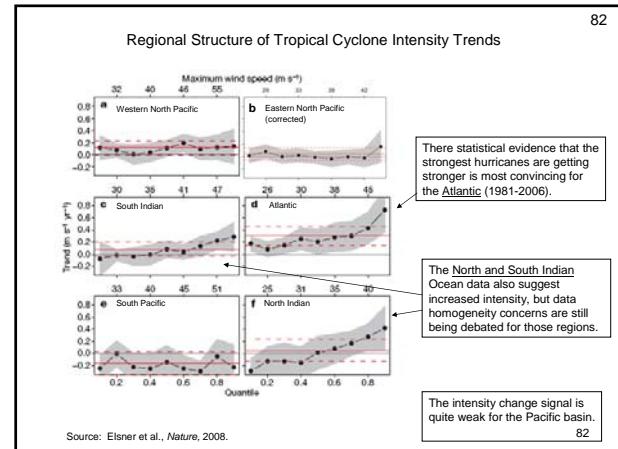


Recent TC Intensity Trends

There is some statistical evidence that the strongest hurricanes are getting stronger. This signal is most pronounced in the Atlantic. However, the satellite-based data for the global analysis are only available for 1981-2006.

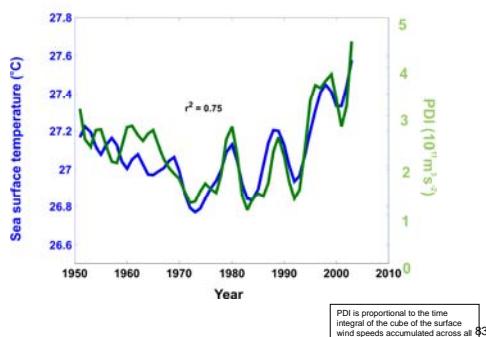
Quantile regression computes linear trends for particular parts of the distribution. The largest increases of intensity are found in the upper quantiles (upper extremes) of the distribution.

Source: Elsner et al., Nature, 2008



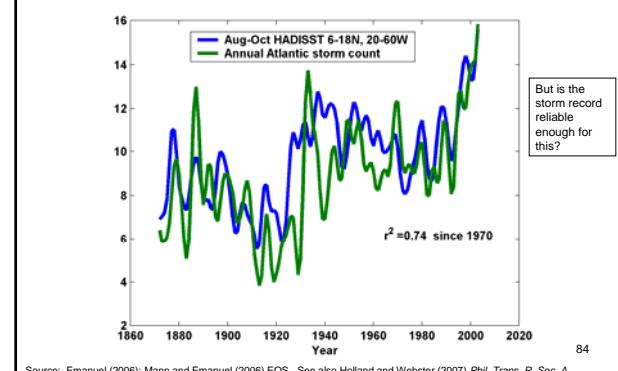
82

There is some recent evidence that overall Atlantic hurricane activity may have increased since in the 1950s and 60s in association with increasing sea surface temperatures...

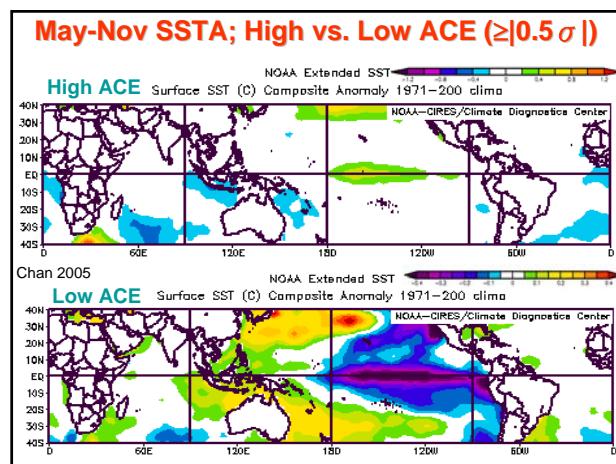
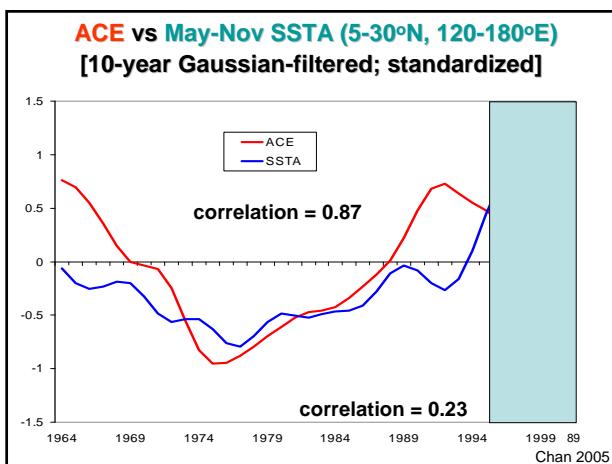
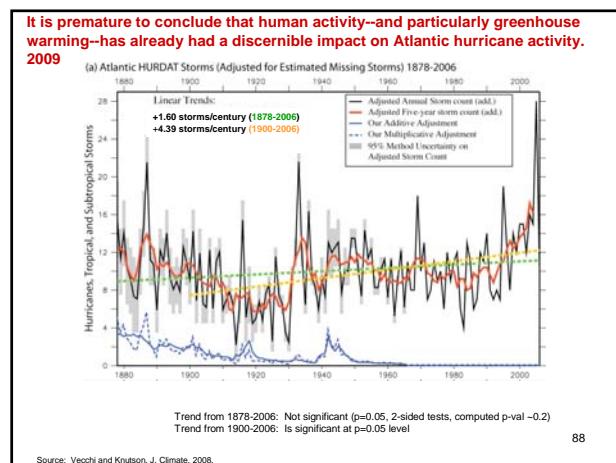
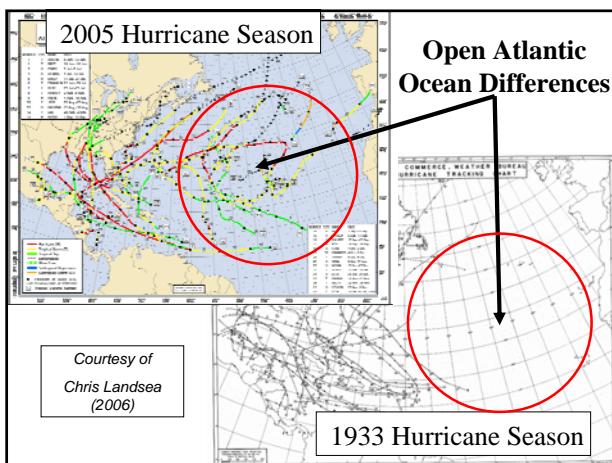
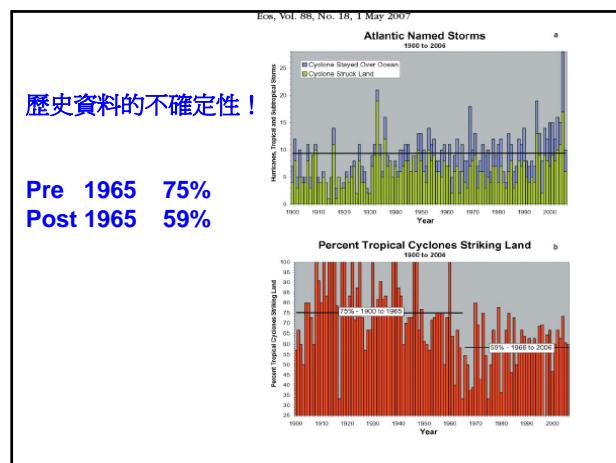
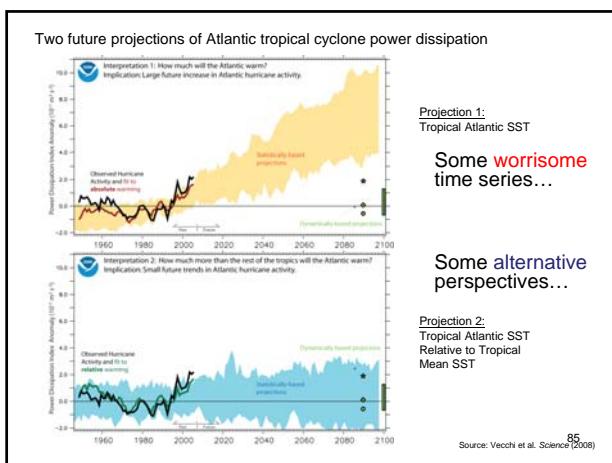


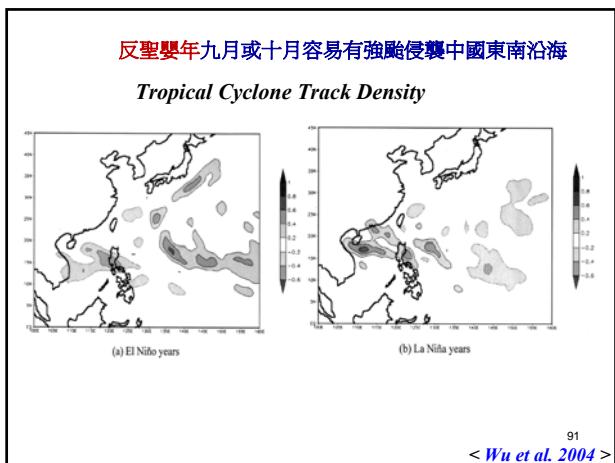
83

The frequency of recorded storms (low-pass filtered) in the Atlantic basin is well-correlated with tropical Atlantic SSTs



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臺灣氣候問題 季節、十年、百年尺度

颱風是關鍵

生成頻率是否有改變？

『目前大多數模式仍無法模擬颱風生成。』

強度與生命期？

『目前大多數模式仍無法合理模擬颱風雙眼牆過程。』

『生成區域與生成頻率之關係？』

『問颱風大小強度，誰主浮沈？』

臺灣未來降雨？

『目前大多數模式無法做出颱風合理雨量。』

生成區域與路徑是否會改變？

『革命尚未成功，同志仍須努力。』

92

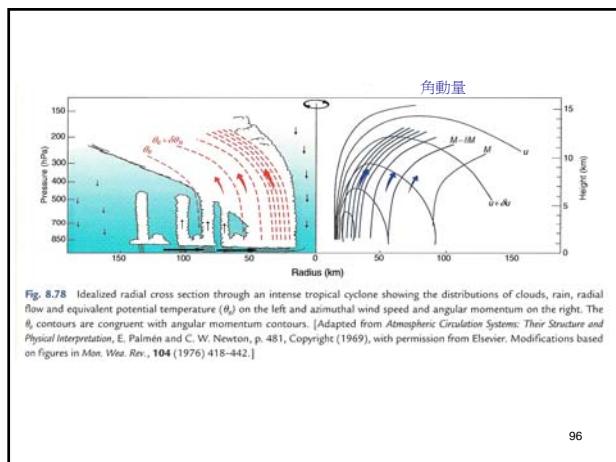
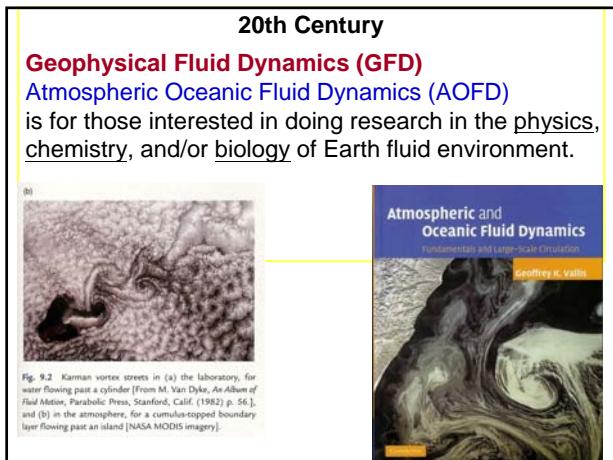




Fig. 8.76 The eye of Hurricane Isabel, passing to the northeast of Puerto Rico at 1315 UTC September 12, 2003. At the time Isabel was a category 5 storm with sustained winds of $\sim 70 \text{ m s}^{-1}$. The eyewall clouds slope radially outward with increasing height. Lower clouds within the eye itself are arranged in a symmetric pattern. [NOAA GOES-12 Satellite imagery.]



Fig. 8.77 The eye of Category-5 Hurricane Katrina late afternoon August 28, 2005 as viewed from an aircraft flying at an altitude $\sim 3.5 \text{ km}$. The photograph was taken looking toward the east just to the south of the center of the eye. The darker clouds are shaded by the western eyewall cloud. The top of the eyewall cloud slopes radially outward with increasing height like the bleachers in a stadium. [Courtesy of Bradley F. Smull and RAINEX.]

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颱風大小與強弱無明顯關係 What are the controls??

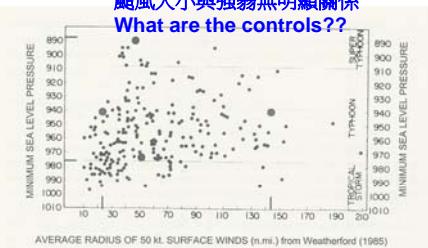


Figure 13. Intensity (minimum sea-level pressure) versus the radial extent of 50 kt (60 miles/hour) winds in nautical miles (n mi) for northwest Pacific typhoons as measured by reconnaissance aircraft [Weatherford and Gray 1988]. One n mi is equal to 1.85 km. Large dots illustrate the large differences that can exist for cyclones of the same minimum sea-level pressure (MSLP) of 940 mb, 23 kt versus 144 kt. Note also that the cyclones of similar outer radius of 50 knot winds can have MSLP differences as great as 890 versus 975 mb. These measurements are also typical of the Atlantic.

Weatherford and Gray 1988

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象神颱風侵襲後的台北市



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臺灣的颱風洪水災害

- 自1897年至2004年間侵臺颱風共計401次，平均每年達3.75次颱風。
- 近40年來颱風所造成之平均年損失達174億元，約為國民生產毛額之0.33%。
- 臺灣與颱洪
 - 有颱風有災害
 - 無颱風無水用
 - 颱風假經濟衝擊上百億



100

中央氣象局都卜勒氣象雷達網



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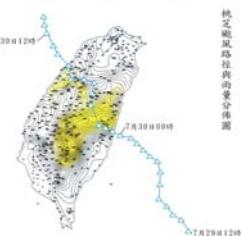
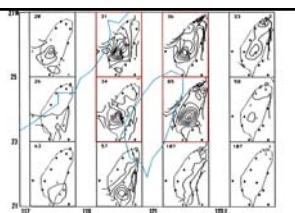
24至36小時前有能力預測數十至近百公里豪大雨區域（地形鎖住效應）

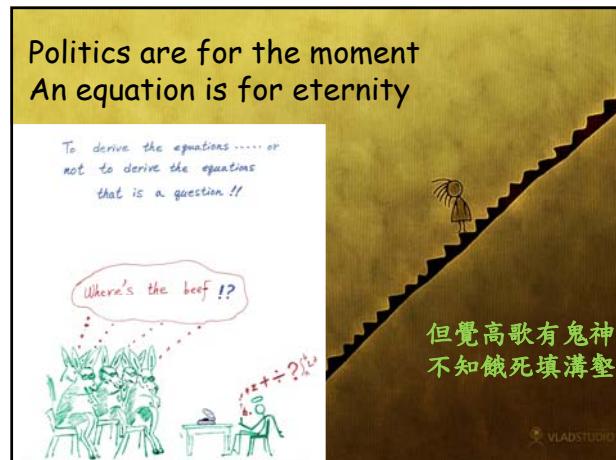
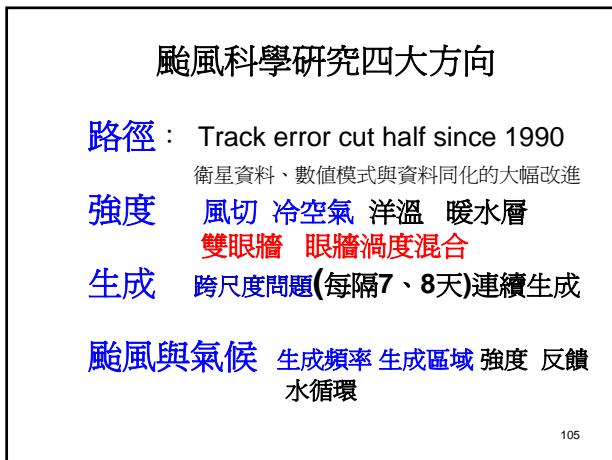
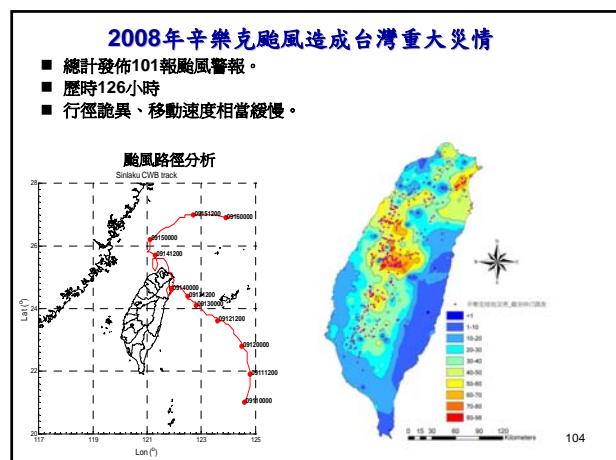
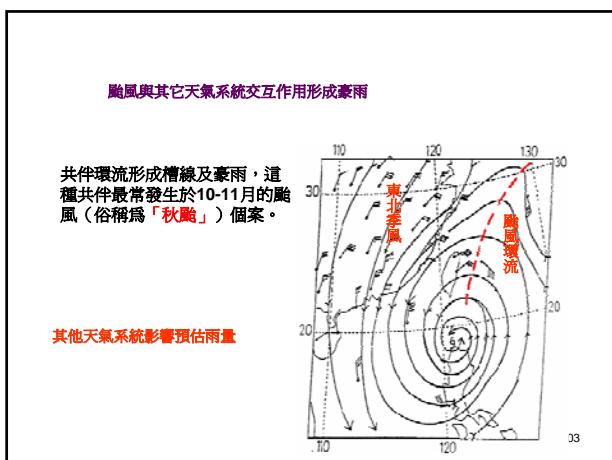
數小時與數十公里範圍中小尺度的氣象預報仍是挑戰

2001年潭美颱風，無預警情形下，中尺度對流，五小時下355mm豪雨，重創高雄市。2008年卡玫基颱風重創中南部

24-72小時路徑預報（颱風來不來？）

水門關閉時機
停班停課與停止活動
考試舉行與否





熱力學 + 流體力學

Euler 1755

$$\frac{d}{dt} \int_{v_m} \rho \vec{v} \, dv = - \int_{\partial v_m} p \, d\vec{s}$$

$$\int_{v_m} \rho \frac{d\vec{v}}{dt} \, dv = - \int_{v_m} \nabla p \, dv$$

$$\rho \frac{d\vec{v}}{dt} = -\nabla p$$

Lagrange 1781

$$\frac{\partial \vec{u}}{\partial t} + \vec{\zeta} \times \vec{u} = -\frac{1}{\rho} \nabla p - \nabla K - \nabla \Phi$$

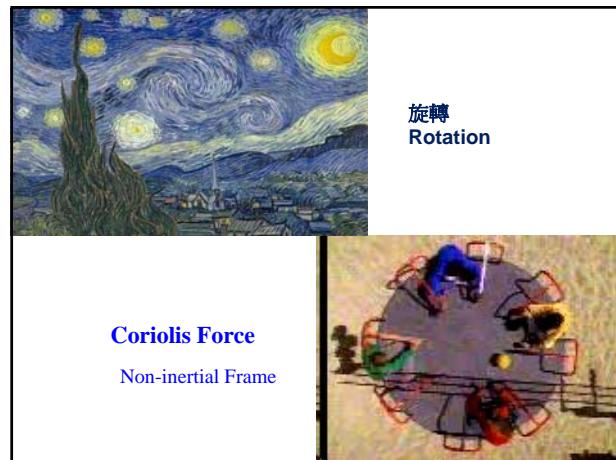
Rotation Vortex

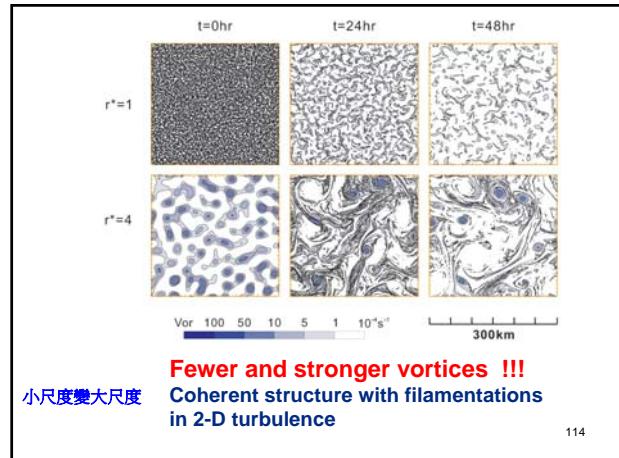
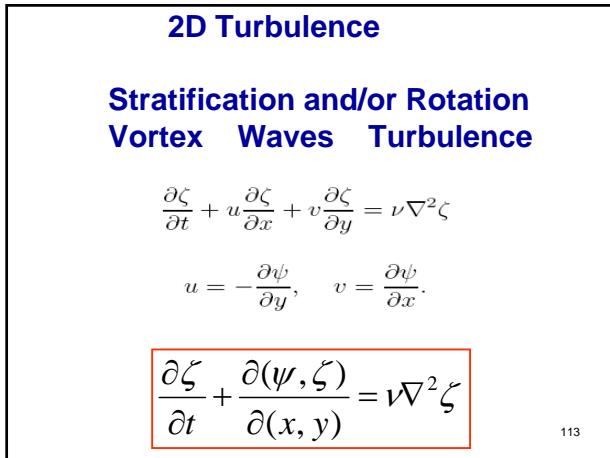
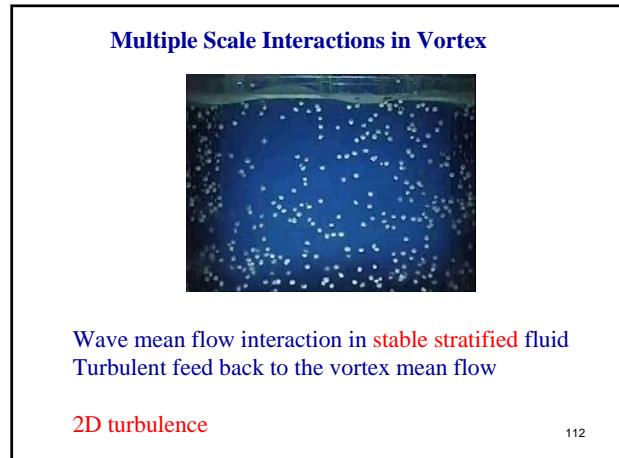
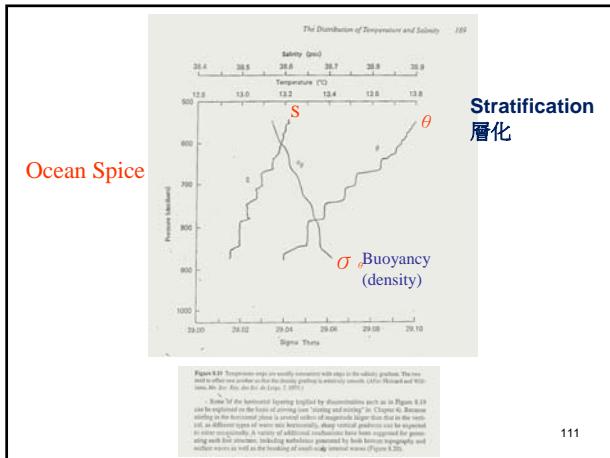
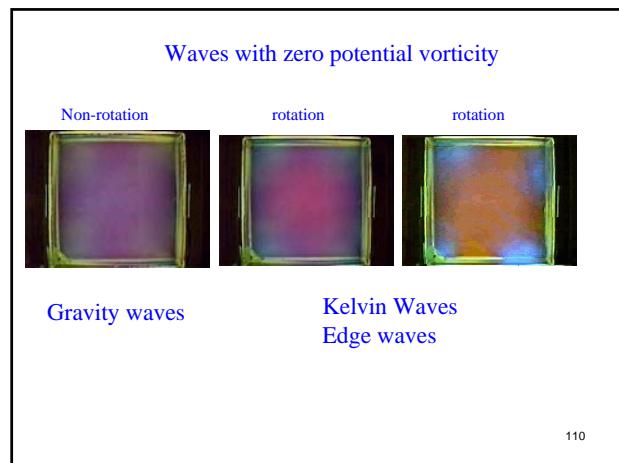
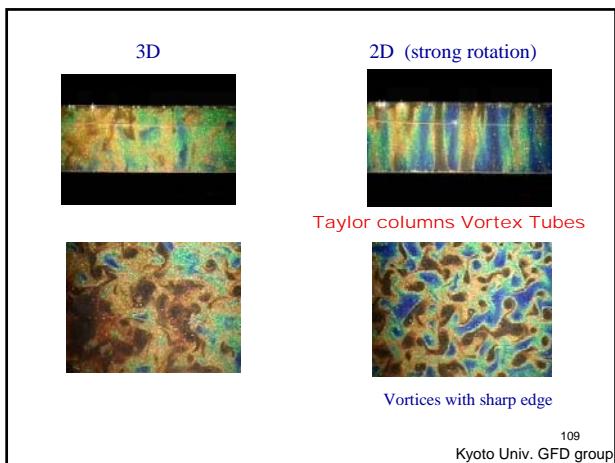
Lorentz Force Law

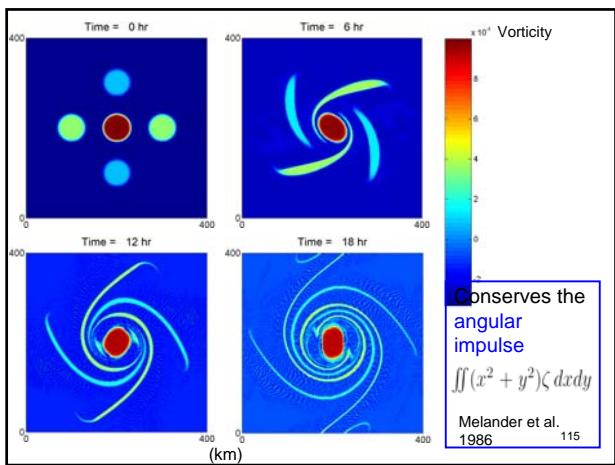
$$\mathbf{F} = q(\mathbf{E} + \mathbf{v} \times \mathbf{B})$$

$$\mathbf{F} = q(-\nabla V + \mathbf{v} \times \mathbf{B})$$

07







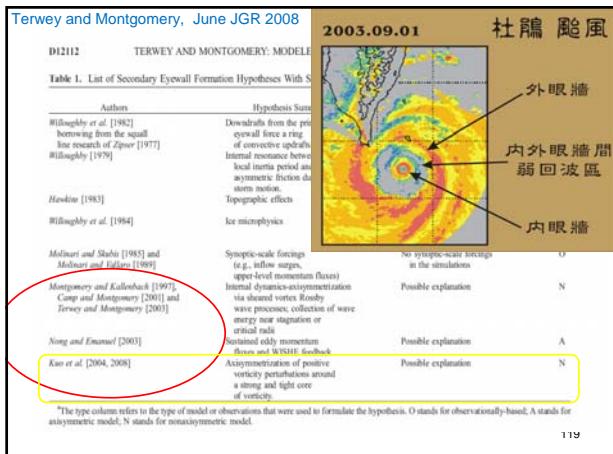
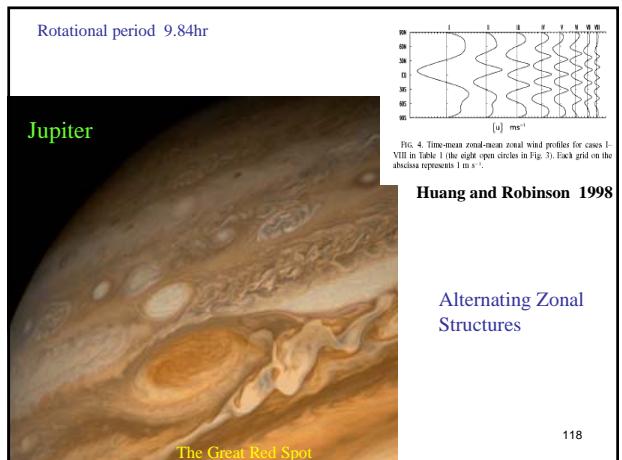
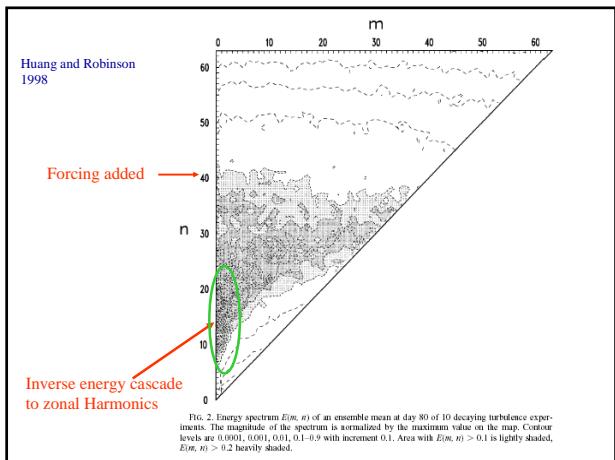
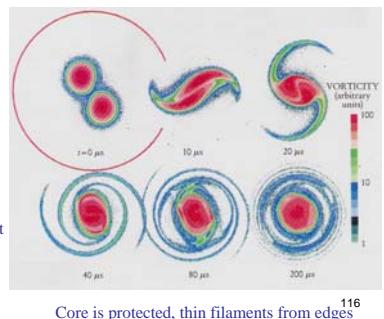
Electron density redistribution in experimental plasma physics

single sign charge
+
axial magnetic field confinement

$$\mathbf{E} = -\nabla\psi$$

$$\nabla \cdot \mathbf{E} = -\nabla^2\psi = \frac{\rho}{\epsilon}$$

\mathbf{B} \mathbf{E} $\vec{\mathbf{E}} \times \vec{\mathbf{B}}$ drift



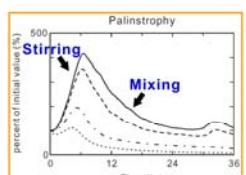
A coffee lover's dream:
The best part of waking up, is the vortex in your cup!

$$\frac{D\theta}{Dt} = \frac{\partial \theta}{\partial t} + \vec{V} \cdot \nabla \theta = v \nabla^2 \theta$$

$$C = \frac{1}{2} \int \nabla \theta \cdot \nabla \theta dV$$

$$\frac{dC}{dt} = \int (\vec{V} \cdot \nabla \theta) \nabla^2 \theta dV - v \int (\nabla^2 \theta) dV$$

Stirring Mixing



Coffee with white

Bowman and Mangus (1993)

臭氧洞衛星觀測

Observations of deformation and mixing of the total ozone field in the Antarctic polar vortex

核心空氣被渦旋鎖住
細絲帶

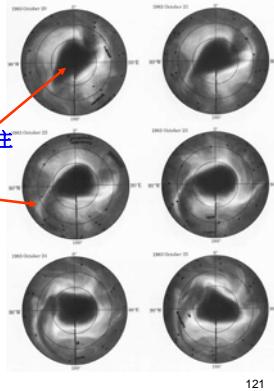


Fig.1: Daily TOMS images of total ozone in the Southern Hemisphere for six consecutive days in October 1983. Latitude circles are drawn at 40°, 60°, and 80° S.



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